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Nuclear Magnetic Resonance Studies of the Phosphorus-31 and Hydrogen-1 Nuclei in Aminophosphonium Compounds

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The phosphorus and proton magnetic resonance spectra of a series of aminophosphonium chlorides have been obtained. The chemical shifts of phosphorus nuclei have been interpreted in terms of electronegativity and π bonding. The chemical shifts of NH₂ protons seem to be related to the basicity of phosphines. In a series of methyl-substituted compounds, J_{PCH_2} remains constant and independent of the nature of other substituent groups on phosphorus. Analytical and infrared data of some new aminophosphonium compounds have been listed.

Synthesis of aminophosphonium chlorides by the chloramination of phosphines has been well established.^{1,2} A number of such compounds have been prepared in our laboratory in this way. Interesting results from the nuclear magnetic resonance spectra of some of these compounds² led us to extend the study in a more systematic way to determine the effect of substitution of different groups on the chemical shifts of **31P** and lH nuclei in these compounds. Though nuclear magnetic resonance data for a number of phosphorus compounds have been published $8-8$ in recent years, most of the available data are for compounds containing oxygen. The reported references are either on ${}^{31}P$ chemical shifts or on proton magnetic resonance of phosphorus compounds. This paper reports a nuclear magnetic resonance study of both **31P** and ¹H nuclei and also the preparation and properties of some of the new aminophosphonium chlorides. Incidently, these are some of the few quaternary phosphorus compounds which contain **N-P** bonds and no oxygen.

Experimental Section

All operations were conducted in a moisture-free nitrogen atmosphere.

Materials.-Solvents used were dried over calcium hydride. Phenyldichlorophosphine and diphenylchlorophosphine were obtained from the Victor Chemical Works, and dimethylamine was obtained from the Matheson Co. Phosphorus trichloride, obtained from J. T. Baker Chemical Co., was redistilled before use.

Analysis.--Elemental analyses were carried out by the Galbraith Microanalytical Laboratories. Melting points were obtained with a Thomas-Hoover capillary melting point apparatus. Analytical and melting point data are listed in Table I.

Infrared Spectra.-The infrared spectra were recorded with a Beckman Model IR 10 grating infrared spectrophotometer. The spectra of solids were taken either in the form of pressed KBr pellets or as Kel-F mulls for the range $2.5-7.5$ μ and as Nujol mulls in the range $7.5-20$ μ . A summary of spectral bands is presented in Table 11.

Nuclear Magnetic Resonance Spectra.--Nuclear magnetic resonance spectra for both ³¹P and ¹H nuclei were determined with a Varian Model V-4300-2 high-resolution spectrometer equipped with a field homogeneity control, magnet insulation, and a superstabilizer, at 19.3 and 60.0 Mcps, respectively. The spectra of liquids were run as pure samples and those of solids were determined either in CDCl₃ or DMSO- d_6 . The proton spectra were referenced by a substitution method, using a 6% solution of tetramethylsilane in chloroform. The field was swept continuously, first through the CHCl₃ peak of the reference tube, then through the peaks of the sample, and finally through the TMS peak. Because of the sensitivity of many of the materials to moisture, an internal standard was not used, and the proton shifts are not to be regarded as reported on the τ scale. ³¹P chemical shifts were determined with respect to H_3PO_4 (85%) as external standard.

Synthesis of Phosphines.---Some of the phosphines used in the present investigation were synthesized as reported in the litcrature. $9-12$ Trimethylphosphine was synthesized by the action of CHsMgI on phosphorus trichloride, distilled along with ether, and the ethereal solution was used as such for chloramination. **Dimethylaminodiphenylphosphine** was prepared by the action of dimethylamine on diphenylchlorophosphine. Diphenylmethylphosphine was synthesized by the action of CHsMgI on diphenylchlorophosphine.

Procedure for Chloramination Reactions.-The chloramine generator used in this study is similar to those described previously.^{13,14} In all of the chloraminations the rates of flow of ammonia, nitrogen, and chlorine into the generator were 1.2: 0.3: 0.1 mole/hr, respectively. The experimental details of a typical reaction are described below.

Diphenylmethylphosphine (0.01 mole) was dissolved in dry ether (60 ml) and exposed to the effluent gases of the chloramine generator. A white precipitate formed immediately in the reactor. The chloramination was continued for **15** min (0.025 mole of chloramine). After the completion of the reaction, the solution was filtered. The solids remaining on the filter were extracted with chloroform. A white material separated from the chloroform solution when an excess of ether was added. This was recrystallized from chloroform (yield 2 .O g) **(79.5%** of theory).

Other aminophosphonium compounds were synthesized in a similar manner.

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ANALYTICAL AND MELTING POINT DATA

Table II

INFRARED DATA $(\text{cm}^{-1})^a$

$[(CH₃)₃PNH₂]$ Cl

3130 s, 3090 s, 3010 s, 2960 s, 2890 s, 2620 w, 2340 w, 1430 sh, m. 1415 m, 1305 sh, w, 1295 s, 1145 w, 1080 w, 1005 s, 965 s, 870 w. 855 w, 775 sh, w, 760 m, 720 m

$[({\rm CH}_{3})_{2}P(C_{6}H_{5})NH_{2}]C1$

3300-2900 b, vs, 2580 vw, 2330 sh, vw, 1620 sh, w, 1580 s, 1490 m, 1430 s, 1405 sh, w, 1310 sh, w, 1300 s, 1195 vw, 1155 sh, w, 1130 s, 995 s, 948 s, 905 w, 872 m, 775 sh, m, 740 s, 685 m, 580 b, m, 470 m, 415 m

$[(CH₃)P(C₆H₅)₂NH₂]Cl$

3200-2720 b, vs, 2560 vw, 2320 vw, 1580 w, 1550 m, 1480 w, 1430 s, 1405 sh, w, 1300 m, 1182 w, 1155 vw, 1115 s, 1040 w, 975 s, 905 s, 890 sh, m, 775 sh, m, 740 s, 715 m, 685 s, 498 s, 475 m, 460 m

$[(CH₃)₂NP(C₆H₅)₂NH₂]Cl$

3120 b, vs, 2940 b, vs, 2530 vw, 2320 vw, 1582 m, 1560 sh, m, 1548 s, 1535 sh, m, 1475 w, 1432 s, 1335 vw, 1295 s, 1168 s, 1115 vs, 1065 m, 992 vs, 952 s, 870 sh, w, 850 sh, w, 760 m, 725 s, 690 s, 538 s, 500 s, 445 w, 415 m

$[[(CH_3)_2N]_2P(C_6H_5)NH_2]Cl$

3120 b, s, 2950 b, s, 2530 vw, 2310 vw, 1582 w, 1540 m, 1480 w, 1445 sh, w, 1435 s, 1415 sh, w, 1290 s, 1195 sh, w, 1180 w, 1162 s, 1125 s, 1065 m, 995 d, vs, 960 s, 880 vw, 780 m, 745 s, 730 m, 700 m, 650 w, 505 s

$[[(CH_3)_2N]_2P(CH_3)NH_2]$ Cl

3300-2700 b, s, 2560 vw, 2320 vw, 1560 m, 1545 w, 1465 sh, 1445 b, m, 1320 w, 1295 s, 1175 s, 1160 s, 1110 vw, 1070 s, 985 b, s, 910 m, 870 sh, w, 790 s, 760 s, 745 m, 725 s, 625 w, $460 b. w$

 α s, strong; m, medium; w, weak; sh, shoulder; d, doublet; b, broad.

Results and Discussion

The nuclear magnetic resonance data are presented in Tables III and IV. In general, for proton magnetic resonance spectra of these compounds, CDCl₃ was used as solvent. However, in cases where the compounds are not sufficiently soluble in CDCl₃, DMSO- d_6 was used. As far as possible, only one solvent was used to compare the spectral data in a particular series. In each case for which the chemical shifts and coupling constants are listed, the spectra were well resolved and the absorptions possessed the expected multiplicity. In only a few cases, the absorption signals for $NH₂$ protons appeared as doublets, but otherwise they appeared as singlets. In the multiplet pattern for each of the phenyl groups, the chemical shift reported corresponds to the strongest peak. The 31P chemical shifts are found to be slightly dependent upon the sol-

TABLE III

NMR PARAMETERS FOR PHOSPHINES

^a Nmr data reported previously. See ref 6 for compounds I and II and ref 8 for compounds V-VII. \rightarrow Nmr data reported previously. ^c J. R. Van Wazer, C. F. Callis, J. N. Shoolery, and R. C. Jones, J. Am. Chem. Soc., 78, 5715 (1956). d W. A. Henderson and S. A. Buckler, ibid., 82, 7591, 5794 (1960). • See ref 5. ^f L. Maier, *Helv. Chim. Acta*, 46, 2667 (1963).

vents used; e.g., the chemical shift of ³¹P in $[(C_6H_5)_3$ - PNH_2]Cl in DMSO is found to be -30.0 ppm while in $CHCl₃$ it is -32.0 ppm. The effect of change in concentration on the ³¹P chemical shift is found to be negligible within the limit of accuracy, which is about ± 1.0 ppm.

It is worthwhile to examine the chemical shifts of ³¹P nuclei in various aminophosphonium compounds, shown in Table IV, with respect to the chemical shift of triphenylaminophosphonium chloride. If each of the phenyl groups is replaced by an $NH₂$ group, there is apparently no change in the chemical shifts. This is also true for methylaminophosphonium chlorides as indicated when the chemical shifts of $[(CH₃)₂P(NH₂)₂]$ -Cl (-42.3 ppm) and [$(CH_3)_2P(C_6H_5)NH_2]Cl$ (-42.8 ppm) are compared. Successive replacement of phenyl groups by methyl groups results in a downfield shift of phosphorus. Each methyl group seems to contribute an amount of about -6.6 ppm to the downfield shift. This is in agreement with an earlier observation⁵ on quaternary phosphorus compounds, where the replacement of one phenyl group by one methyl group causes a shift of -8.0 ppm.

Substitution of a dimethylamino group for a phenyl group (series III) causes a downfield shift of ³¹P nuclei from -30.0 ppm in $[(C_6H_5)_3$ PNH₂]Cl to -40 ppm in $[(C_6H_5)_2P[N(CH_3)_2]NH_2]Cl.$ However, further replacement of phenyl groups by dimethylamino groups does not have any effect on the chemical shift. An irregular trend is also observed when a methyl group is replaced by a dimethylamino group (series IV). There seems to be no quantitative correlation between chemical shift and nature of the group attached in this series of compounds, since the observed shifts of

Compound	Solvent for pmr	TC_6H_5	TNE ₂	TCH_3	TNCH ₂	J PCH, cps	J_{PNCH} cps	$\delta^{31}P$ ppm	Solvent for $31P$ nmr
			Series I						
$[(C_6H_5)_3PMH_2]Cl^a$	CDCl ₃	2.36	2.68					-32.0	CHCl ₂
	DMSO	2.42	2.87					-30.0	DMSO
$[(C_6H_6)_2P(CH_3)NH_2]$ Cl	CDC1.	2.55	3.0	7.43		14.1		-38.0	DMSO
$[(C_6H_5)P(CH_3)_2NH_2]Cl$	CDCl ₃	2.45	3.7	7.78		14.5		-42.8	DMSO
$[(CH3)3PNH2]C1$	$DMSO-d_8$		4.74	8.19		14.5		-49.6	DMSO
				Series II					
$[(C_6H_6)_8PMH_2]$ C1	DMSO	2.42	2.87					-30.0	DMSO
$[(C_6H_5)_2P(NH_2)_2]Cl^b$	$DMSO-d_6$	2.44	3.78					-31.9 ± 2	DMSO
$[({\rm C}_6{\rm H}_6){\rm P}({\rm NH}_2)_3]$ Cl ^b	$DMSO-d_8$	2.47	4.58					-29.4	DMSO
				Series III					
$[(C_6H_5)_3PNH_2]C1$	CDCl ₃	2.36	2.68					-32.0	CHCl ₂
								-30.0	DMSO
$[(C_6H_5)_2P[N(CH_3)_2]NH_2]Cl$	CDCl ₃	2.35	2.95		7.05		11.7	-42.2	CHCl ₃
								-39.9	DMSO
$[(C_6H_6)P[N(CH_3)_2]_2NH_2]$ Cl	CDCl ₃	2.35	2.88		7.15		10.4	-43.0	CHCl _s
								-41.0	DMSO
$[(CH_3)_2N]_3PNH_2]Cl^c$	CDCl ₃		3.66		7.11		9.5	-42.6	CHCl ₃
								-39.0	DMSO
				Series IV					
$[(CH_3)_3 PNH_2]$ C1	$DMSO-d_6$		4.74	8.19		14.5		-49.6	DMSO
$[({\rm CH}_{3})_{2}P[{\rm N}({\rm CH}_{3})_{2}]{\rm NH}_{2}]{\rm Cl}^{d}$	CDCl ₃		3.70	7.8	7.08	14.5	11.1	-54.0	CHCl ₃
$[(CH3)P[N(CH3)2]$ ₂ NH ₂]Cl	CDCl ₃		3.57	8.0	7.16	14.8	9.9	-53.0	CHCl ₃
$[(CH3)2N]3PNH2]Cl$	CDCl ₃		3.66		7.11		9.5	-42.6	CHCl ₃
				Series V					
$[(CH3)2P(NH2)2]Cle$	$DMSO-d_6$		4.8	8.37		14.2		-42.3	DMSO
NH ₂ Cl	$(C_2H_6)_2O$		6.26						

TABLE IV NMR PARAMETERS FOR AMINOPHOSPHONIUM SALTS

^a Synthesis reported in ref 1. ^b Synthesized by S. E. Frazier and H. H. Sisler, *Inorg. Chem.*, **5,** 925 (1966). *c* Analytical data to be published. ^d Data from the Ph.D. thesis of D. F. Clemens, University of Florida, 1965. Synthesized by H. H. Sisler and S. E. Frazier, *Inorg. Chem.,* **4,** 1204 (1965).

 $[(CH_3)_2N]_2P(CH_3)NH_2]Cl$ and $[(CH_3)_2NP(CH_3)_2$ - $NH₂$ C1 are more downfield than either tris(dimethylamino) or trimethyl derivatives.

Comparison of these data on the chemical shifts of 31P nuclei broadly indicate that the shielding of phosphorus varies with the substituent group as: $C_6H_5 \simeq$ $NH₂ > N(CH₃)₂ > CH₃$. Since both $NH₂$ and $N(CH₃)₂$ groups are more electronegative than the phenyl group, this order is consistent with the recent work of Letcher and Van Wazer¹⁵ in which it was established that, for quaternary phosphorus compounds, there is a substantial contribution to the chemical shift from the amount of π bonding, as well as from the electronegativity. These two factors operate in such a way that an increase in electronegativity of the group increases the shielding and an increase in bond order resulting from π bonding reduces the shielding. These authors have also calculated the amount of π bonding in compounds of the type MPZ_3 where $M = 0$, S, or Se and have reported considerable π bonding in the compounds having $Z = NH_2$ or $N(CH_3)_2$ groups. In the present case, more shielding of ³¹P nuclei in $[(C_6H_5)_3PNH_2]Cl$ than in $[(CH_3)_8PNH_2]Cl$ might be explained to some extent as resulting from the more electronegative nature of the phenyl group than of the methyl group. However, in the case of compounds having an amino or

dimethylamino group, the amount of π bonding plays a major role in accounting for the observed chemical shift.

The proton magnetic resonance data for neutral phosphines and their aminophosphonium salts are listed in Tables I11 and IV. **A** downfield shift in proton resonances, particularly in $P - CH_3$ protons, in all phosphonium compounds reflects an expected decrease in electron density on the phosphorus resulting from quaternization. Assuming that an upfield shift reflects an increase in electron density, an order of base strengths of phosphines may be derived from the $NH₂$ proton resonances of the aminophosphonium compounds. From the chemical shifts, two sequences of the tendency of phosphines to donate electrons to the amino group can be deduced: $(CH_3)_3P > (CH_3)_2P$ - $(C_6H_5) > CH_3P(C_6H_5)_2 > (C_6H_5)_3P$ and $(CH_3)_3P >$ $[({\rm CH}_3)_2N]_3P > (C_6H_5)_3P$. These sequences are in accord with the order of basicity of phosphines as reported in the literature.^{16,17}

The magnitudes of the coupling constants J_{PCH} and J_{PNCH} increase when the phosphorus atom is quaternized. This change in magnitude in J_{PCH} is associated with increased s character in $P-C$ bonds⁸ resulting from quaternization, in the course of which the bonding (16) W. **A.** Henderson and S. **A.** Buckler, *J. Am. Chem. Soc., 78,* 5715 (1956).

(15) J. H. Letcher and J. R. Van Wazer, *J. Chem. Phys.,* **44,** 815 (1966).

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orbitals change from **p3** to sp3. At the same time, substitution of the more electronegative NH₂ group on the phosphorus atom is expected to divert additional s character into P-C bonds.^{6,8} The increment in J_{PCH} with increase in s character is also observed in the case of phenyl- and dimethylamino-substituted methylphosphines as given in Table 111. These results seem to contradict those of Manatt, *et a1.,18* who found that for methyl-substituted phosphines increase in s character decreases the magnitude of J_{PCH} . However, it is possible that the sign of this coupling constant may differ in the phosphines from that in the phosphonium salt.

It is interesting to note that the values of the J_{PCH} coupling constants remain constant $(14.4 \pm 0.3 \text{ cps})$ in a series of methyl-substituted aminophosphonium chlorides regardless of the other substituents on the phosphorus atom. Similar results have also been obtained by earlier workers $6,7$ on some other methyl-substituted phosphonium salts. This constancy is also observed to a smaller degree in the case of $J_{\rm PNCH}$, the magnitude of which is 10.6 ± 1.1 cps.

Whereas the chemical shifts of $(CH_3)_2N$ protons are almost unaffected by other substituents on the phosphorus atom $(\tau 7.11 \pm 0.06)$, the chemical shifts of $CH₃$ protons show appreciable change with the other substituents on the phosphorus. This probably results from the $(CH_3)_2N$ protons being, three bonds (P-N-C-H) away from phosphorus and therefore not

(18) *S.* L. Manatt, G. L. Juvinall, R. I. Wagner, and D. D. Elleman, *J. Am. Chem. Soc., 88,* 2689 (1966).

much affected by the change in electron density on the phosphorus atom caused by the other substituent. Also, spectra of methyldimethylaminophosphonium chlorides, on comparison with those of the corresponding phosphines, show a large downfield shift of $P-CH_3$ protons and large increment in J_{PCH} on quaternization, thus suggesting that, as concluded by earlier workers² from other evidence, chloramination occurs on the phosphorus atom rather than the nitrogen atom.

Infrared spectra of the new aminophosphonium chlorides prepared during the course of this investigation are summarized in Table 111. These spectra are similar to spectra of other phosphonium salts as reported earlier² and the spectral bands can be assigned accordingly. The general occurrence of a strong band in the region 1290-1300 cm^{-1} in all of these compounds probably results from P-CH₃ or P-N(CH₃)₂ vibrations.¹⁹ The strong absorptions in the region of $980-950$ cm⁻¹ in dimethylaminophosphines have been assigned to the $P-N(CH_3)$ ² group;¹² this band appears in the range 995-950 cm^{-1} in the spectra of aminophosphonium chlorides.

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An Investigation of the Boron-Nitrogen Bonds in Some Aminoboranes

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Simple Hückel calculations have been carried out in order to assess relative π -bond orders of the B-N bonds in a series of aminoboranes with various substituents. The results are shown to correlate well with relative bond orders as deduced from infrared stretching frequencies. The B^{11} nmr chemical shifts are also found to be related to the π -electron densities calculated for the boron atoms.

The nature of B-N bonds in aminoboranes has recently been of considerable interest.^{2,3} In 1948⁴ Wiberg postulated that the filled p orbital of the nitrogen atom and the empty p orbital of the boron atom might be involved in forming a partial double bond in aminoboranes. The double-bond character of the B-N linkage may thus result in *cis-trans* isomerism in a substituted aminoborane, e.g.

(1) Department of Chemistry, University of Florida, Gainesville, Fla. (2) K. Niedenzu and J. W. Dawson, "Boron-Nitrogen Compounds," Academic Press Inc., New York, N. *Y.,* 1965, pp 48-65.

(3) K. Niedenzu, *Angew. Chem.,* **3,** 86 (1964).

The results of proton magnetic resonance studies of some aminoboranes containing at least one substituent having protons substantiated this hypothesis. $5-10$

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(5) G. E. Ryschkewitsch, W. S. Brey, Jr., and **A.** Saji, *J. Ant. C'hem. Soc.,* **83,** 1010 (1861).

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(8) P. A. Barfield, M. F. Lappert, and J. Lee, *Proc. Chem.* Soc., 421 (1961).

(9) W. *S.* Brey, Jr., K. N. Scott, and M. R. Chakrabarty, "Restricted Rotation in Some Aminoboranes," Abstracts of Southeast-Southwest Regional Meeting of the American Chemical Society, Memphis, Tenn., Dec 1965.

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